

# ROBERT KRONE

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## EMPLOYMENT

2017–2020 Krener Assistant Professor, **University of California - Davis**  
2015–2017 Postdoctoral Fellow, **Queen’s University**

## EDUCATION

2020–2020 Fellowship program in Data Science, **The Data Incubator**  
2010–2015 Ph.D. in Mathematics, **Georgia Institute of Technology**  
Advisor: Anton Leykin  
Thesis: “Symmetric ideals and numerical primary decomposition”  
Minor: Computer Science  
2004–2008 B.A. in Mathematics, **Princeton University**  
Certificate in Computer Science

## RESEARCH INTERESTS

Applied algebraic geometry: using algebraic geometry tools to solve applied problems, and developing computational tools such as software packages for solving algebraic problems.

## PAPERS

Justin Chen, Yairon Cid-Ruiz, Marc Härkönen, Robert Krone, Anton Leykin. Noetherian operators in Macaulay2, *preprint* arXiv:2101.01002 (2021).  
Mareike Dressler and Robert Krone. Multiple typical ranks in matrix completion, *preprint* arXiv:2010.09777 (2020).  
Justin Chen, Marc Härkönen, Robert Krone, Anton Leykin. Noetherian operators and primary decomposition, *preprint* arXiv:2006.13881 (2020).  
Robert Krone and Kaie Kubjas. Uniqueness of nonnegative matrix factorizations by rigidity theory, *SIAM Journal on Matrix Analysis and Applications* 42.1, pages 134-164 (2021).  
Daniel Irving Bernstein and Robert Krone. The tropical Cayley-Menger variety, *SIAM Journal on Discrete Mathematics* 33.3, pages 1725-1742 (2019).  
Jesús A. De Loera, Serkan Hoşten, Robert Krone, Lily Silverstein. Average Behavior of Minimal Free Resolutions of Monomial Ideals, *Proceedings of the American Mathematical Society* 147.8, pages 3239-3257 (2019).  
Hector Baños, Nathaniel Bushek, Ruth Davidson, Elizabeth Gross, Pamela E Harris, Robert Krone, Colby Long, Allen Stewart and Robert Walker. Dimensions of Group-

based Phylogenetic Mixtures, *Bulletin of Mathematical Biology* 81, pages 316–336 (2018).

Madeline Brandt, DJ Bruce, Taylor Brysiewicz, Robert Krone and Elina Robeva. The degree of  $SO(n)$ , *Combinatorial Algebraic Geometry* (book), pages 229–246 (2016).

Hector Baños, Nathaniel Bushek, Ruth Davidson, Elizabeth Gross, Pamela E Harris, Robert Krone, Colby Long, Allen Stewart and Robert Walker. Phylogenetic Trees, *Journal of Software for Algebra and Geometry* 11.1, pages 1–7 (2021).

Chris Hillar, Robert Krone and Anton Leykin. Equivariant Gröbner bases, *The 50th Anniversary of Gröbner Bases* (book), pages 129–154 (2018).

Robert Krone, Anton Leykin and Andrew Snowden. Hilbert series of symmetric ideals in infinite polynomial rings via formal languages, *Journal of Algebra* 485, pages 353–362 (2016).

Robert Krone. Equivariant Gröbner bases of symmetric toric ideals, *In Proceedings of the 41th International Symposium on Symbolic and Algebraic Computation, ISSAC '16*, pages 311–318 (2016).

Robert Krone and Anton Leykin. Numerical algorithms for detecting embedded components, *Journal of Symbolic Computation* 82, pages 1–18 (2017).

Robert Krone and Anton Leykin. Eliminating dual spaces, *Journal of Symbolic Computation* 79, pages 609–622 (2017).

Thomas Kahle, Robert Krone, Anton Leykin. Equivariant lattice generators and markov bases, *In Proceedings of the 39th International Symposium on Symbolic and Algebraic Computation, ISSAC '14*, pages 264–271 (2014).

Jan Draisma, Rob Eggermont, Robert Krone, Anton Leykin. Noetherianity for infinite-dimensional toric varieties, *Algebra & Number Theory* 9.8, pages 1857–1880 (2015).

Robert Krone. Numerical algorithms for dual bases of positive-dimensional ideals, *Journal of Algebra and Its Applications* 12.6 (2013).

## SOFTWARE

`PhylogeneticTrees` package for Macaulay2 computer algebra system for computing invariants of statistical models for evolutionary phylogenetic trees.

`RegularLanguages/OIModules` a package for Macaulay2 computer algebra system for working with regular languages and finite state automata, used for equivariant Hilbert series computation.

`NoetherianOperators` package for Macaulay2 computer algebra system for using differential operators to represent the multiplicity structure of primary components of schemes, and numerically computing local Hilbert functions.

`EquivariantGB` package for Macaulay2 computer algebra system for computing equivariant Gröbner bases of algebraic systems with symmetric group symmetry.

## VISITING PROGRAMS

Sep–Dec 2018 ICERM Semester Program - Nonlinear Algebra (Brown University)

Aug–Sep 2016	Fields Institute Program - Combinatorial Algebraic Geometry apprenticeship weeks (University of Toronto)
Oct–Dec 2015	Fields Institute Program - Computer Algebra (University of Toronto)
Oct–Nov 2014	Simons Institute Program - Algorithms and Complexity in Algebraic Geometry (UC Berkeley)
Jul 2014	IMA PI Summer Program - Modern Applications of Representation Theory (University of Chicago)
Mar–Jun 2013	Research visit with Jan Draisma (TU Eindhoven)
Jun–Jul 2012	IMA PI Summer Program - Algebraic Geometry for Applications (Georgia Tech)

## HONORS AND AWARDS

2016	Best Thesis Award, Georgia Institute of Technology - School of Mathematics
2015	Top Graduate Student Award, Georgia Institute of Technology - School of Mathematics
2014 Spring	Algorithms & Randomness Center Student Fellowship, Georgia Institute of Technology
2010–2014	President’s Fellowship, Georgia Institute of Technology

## SERVICE

Spring 2020	Bay Area Discrete Math Day - co-organizer
Apr 2020	AMS Western Sectional mini-symposium on Algebraic Geometry in Statistics and Machine Learning - co-organizer
Winter 2018	UC Davis Mathematics for Data Science and Decision Making seminar - organizer
Fall 2018	ICERM Nonlinear Algebra postdoc seminar - co-organizer
Jul 2017	SIAM Conference on Applied Algebraic Geometry mini-symposium on Theory of Numerical Algebraic Geometry - co-organizer
Jan 2017	AMS Joint Meeting mini-symposium on Numerical Algebraic Geometry - co-organizer
2012–2013	Georgia Tech Research Horizons seminar - co-organizer
2010–2014	Georgia Tech High School Math Competition - problem writer and grader

## INVITED TALKS AND POSTERS

Sep 2019	AMS Central Sectional Meeting (University of Wisconsin) Talk: “Typical coranks”
Sep 2019	San Francisco State University - Algebra Seminar Talk: “Matrices on the nonnegative rank boundary”
Jul 2019	SIAM Conference on Applied Algebraic Geometry (Bern University) Talk: “FI-algebras: examples and counterexamples”
Jul 2019	Summer School on Randomness and Learning in Non-Linear Algebra (MPI Leipzig) Talk: “Predictions and learning with random monomial ideals”
Sep 2018	Conference on Core Computational Methods in Nonlinear Algebra (ICERM) Talk: “Computational tools for FI-algebras”
Aug 2018	Representation Stability Week (University of Michigan) Talk: “Computational tools for FI-algebras”
Jul 2018	SIAM 2018 Annual Meeting (Portland, OR) Talk: “Dimensions of group-based phylogenetic mixtures”
Apr 2018	University of Kentucky - Algebra Seminar Talk: “FI-algebras”
Aug 2017	SIAM Conference on Applied Algebraic Geometry (Georgia Tech)

Jul 2017 Applied Macaulay2 Tutorials (Georgia Tech)  
 Talk: "Modules over FI-algebras"  
 Jan 2017 AMS Joint Mathematics Meeting (Atlanta)  
 Talk: "Degree of  $SO(n)$ "  
 Nov 2016 AMS Southern Sectional Meeting (North Carolina State University)  
 Talk: "The degree of the special orthogonal group"  
 Jul 2016 ISSAC 2016 (Wilfrid Laurier University)  
 Talk: "Hilbert series of infinite symmetric ideals"  
 Jul 2016 SIAM 2016 Annual Meeting (Boston, MA)  
 Talk: "Equivariant Gröbner Bases of Symmetric Toric Ideals"  
 Jun 2016 Georgia Tech - Algebra Seminar  
 Talk: "Hilbert series of invariant ideals"  
 Apr 2016 Free Resolutions, Representations, and Asymptotic Algebra workshop (BIRS)  
 Talk: "Macaulay dual spaces and local Hilbert functions"  
 Feb 2016 York University - Applied algebra seminar  
 Talk: "Equivariant Gröbner bases"  
 Nov 2015 McMaster University - Algebra seminar  
 Talk: "Noetherianity for infinite-dimensional symmetric toric varieties"  
 Oct 2015 Route 81 Conference (Queen's University)  
 Talk: "Numerical Primary Decomposition"  
 Oct 2015 AMS Central Sectional Meeting (Loyola University)  
 Talk: "Equivariant Gröbner bases"  
 Sep 2015 CUNY - Symbolic-Numeric Computing seminar  
 Talk: "Equivariant Gröbner bases of toric ideals"  
 Apr 2015 Meeting on Algebraic Geometry and Applications (Georgia Tech)  
 Talk: "Numerical primary decomposition"  
 Nov 2014 San Jose State University - Combinatorics seminar  
 Talk: "Equivariant Gröbner basis algorithms"  
 Oct 2014 UC Berkeley - Computational Algebraic Geometry seminar  
 Talk: "Finite generation of symmetric toric ideals"  
 Oct 2014 AMS Western Sectional Meeting (San Francisco State)  
 Talk: "Numerically detecting embedded components"  
 Oct 2014 UC Davis - CACAO seminar  
 Talk: "Finite generation of symmetric toric ideals"  
 Sep 2014 University of Georgia - Algebraic Geometry seminar  
 Talk: "Finite generation of symmetric toric ideals"  
 Jul 2014 ISSAC 2014 (Kobe University)  
 Talk: "Equivariant lattice generators and Markov bases"  
 Jul 2014 Workshop on applications of algebraic geometry and algebraic analysis (Kobe University)  
 Talk: "Finite generation of symmetric toric ideals"  
 Jun 2014 Computational Nonlinear Algebra conference (ICERM)  
 Poster: "Numerical Primary Decomposition"  
 Apr 2014 North Carolina State University - Symbolic Computation seminar  
 Talk: "Noetherianity for infinite-dimensional toric ideals"  
 Jan 2014 Macaulay2 Workshop (MSRI - UC Berkeley)  
 Talk: "Equivariant Gröbner Bases"  
 Aug 2013 SIAM Conference on Applied Algebraic Geometry (Colorado State)  
 Talk: "Macaulay Dual Space and Numerical Primary Decomposition"  
 Jun 2013 Effective Methods in Algebraic Geometry 2013 (Goethe-Universität)  
 Talk: "Algorithms for equivariant Gröbner Bases"  
 Jun 2013 DIAMANT Symposium 2013 (Heeze, Netherlands)  
 Talk: "Noetherianity for infinite-dimensional toric varieties"

Mar 2013 Technical University of Eindhoven - Discrete Mathematics seminar  
 Talk: "Computing Equivariant Gröbner Bases"

Oct 2012 RTG Workshop: Tensors and their Geometry in High Dimensions (UC Berkeley)  
 Talk: "Algorithms for symmetric Gröbner bases"

Apr 2012 Texas Algebraic Geometry Symposium 2012 (Texas A&M)  
 Poster: "Numerical algorithms for dual bases of positive-dimensional ideals"

Oct 2011 SIAM Conference on Applied Algebraic Geometry (North Carolina State)  
 Talk: "Numerical algorithms for dual bases of positive-dimensional ideals"

## TEACHING

2020 Winter MATH 150A: Modern Algebra A

2020 Winter MATH 22A: Linear Algebra

2019 Fall MATH 108: Intro to Abstract Math

2019 Spring MATH 16A: Short Calculus A

2019 Winter MATH 108: Intro to Abstract Math

2018 Winter MATH 16B: Short Calculus B

2017 Fall MATH 67: Modern Linear Algebra

2017 Fall MATH 16B: Short Calculus B

2017 Winter MATH 228: Complex Analysis

2016 Fall MATH 221: Vector Calculus

2016 Spring APSC 172: Calculus II

2016 Winter APSC 171: Calculus I

2013 Fall Lead Instructor - MATH 1522: Linear Algebra

2012 Fall Recitation TA - MATH 1512: Honors Calculus II

2012 Spring Recitation TA - MATH 2605: Linear and Discrete Mathematics

2011 Fall Recitation TA - MATH 2605: Calculus III for Computer Science

2011 Spring Recitation TA - MATH 2602: Linear and Discrete Mathematics

2010 Fall Recitation TA - MATH 2602: Linear and Discrete Mathematics

2009–2010 Private Tutor - high school math and science